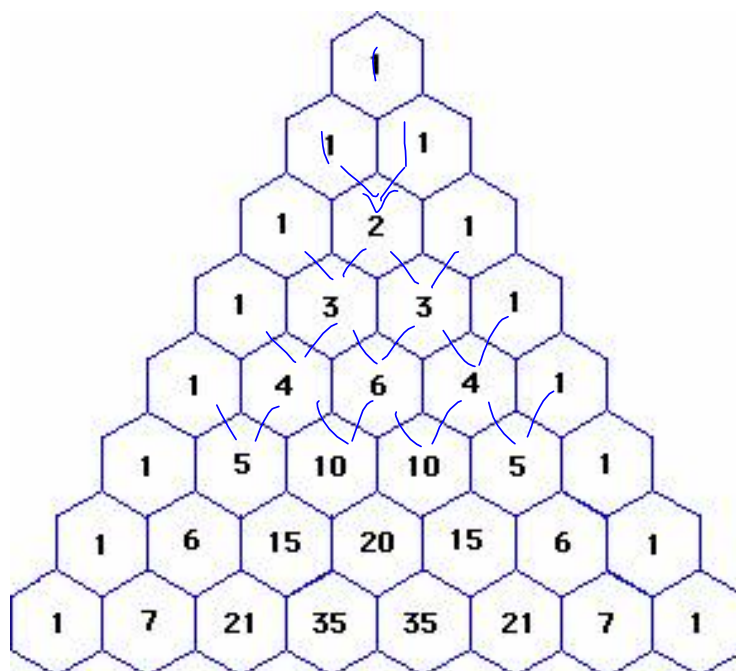


Pascal's Triangle



Investigate
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Pascal's Triangle - Binomial Expansion

row 0

row 1

r 2

r 3

$$(x+y)^6$$

$$= x^6y^0 + 6x^5y + 15x^4y^2 + 20x^3y^3 + 15x^2y^4 + 6xy^5 + x^0y^6$$

1							
1	1						
1	2	1					
1	3	3	1				
1	4	6	4	1			
1	5	10	10	5	1		
1	6	15	20	15	6	1	
1	7	21	35	35	21	7	1

$$(3x + 2y)^4$$

$$1(3x)^4(2y)^0 + 4(3x)^3(2y)^1 +$$

$$6(3x)^2(2y)^2 + 4(3x)^1(2y)^3 + 1(3x)^0(2y)^4$$

$$= 81x^4 + 108x^3y + 216x^2y^2 + 96xy^3 + 16y^4$$

r1	1	1	1			
r2	1	2	1			
r3	1	3	3	1		
r4	1	4	6	4	1	
	1	5	10	10	5	1

$$(x+y)^3$$

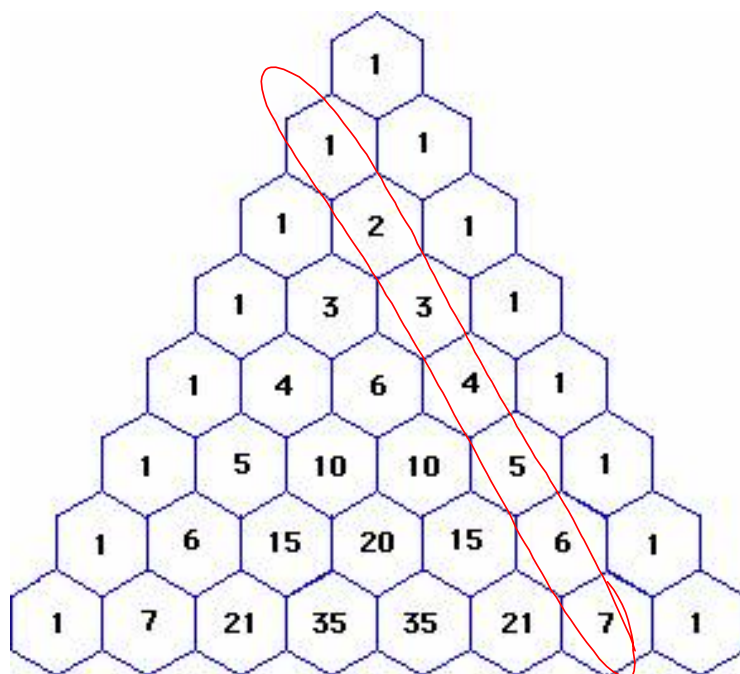
$$= (x+y)(x+y)(x+y)$$

$$= (x^2 + 2xy + y^2)(x+y)$$

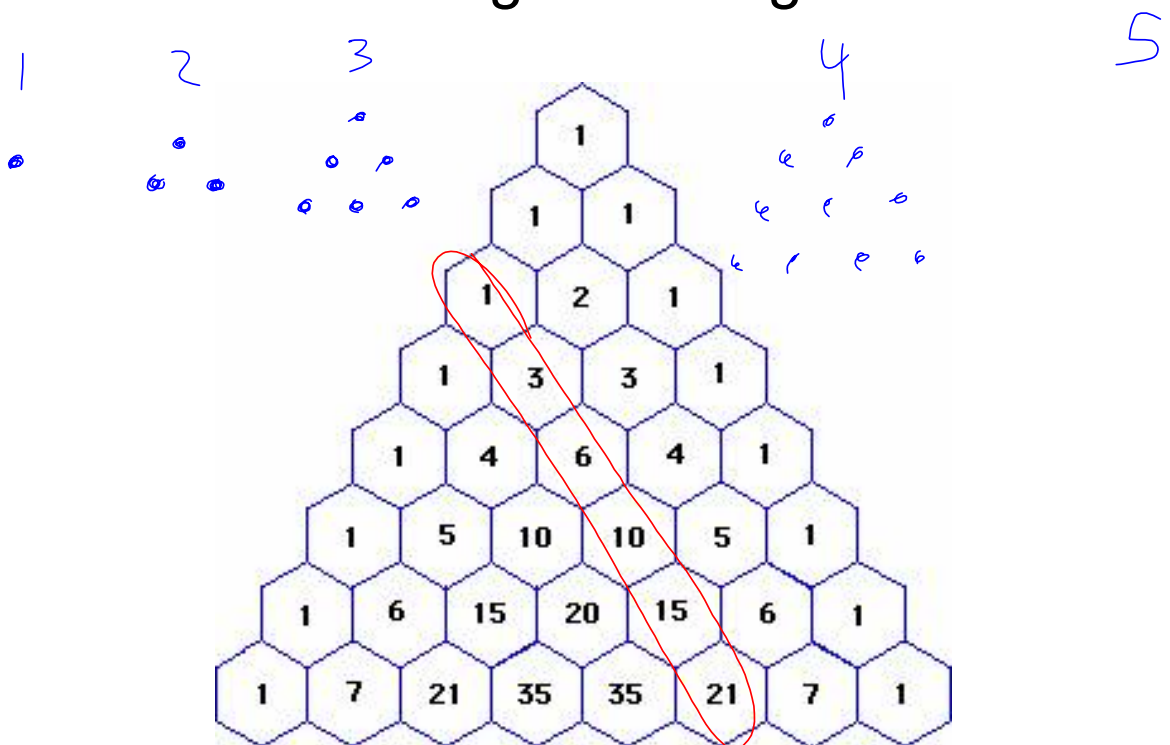
$$(x^3 + \cancel{x^2y} + \cancel{2x^2y} + \cancel{2xy^2} + \cancel{xy^2} + y^3)$$

$$= x^3 + 3x^2y + 3xy^2 + y^3$$

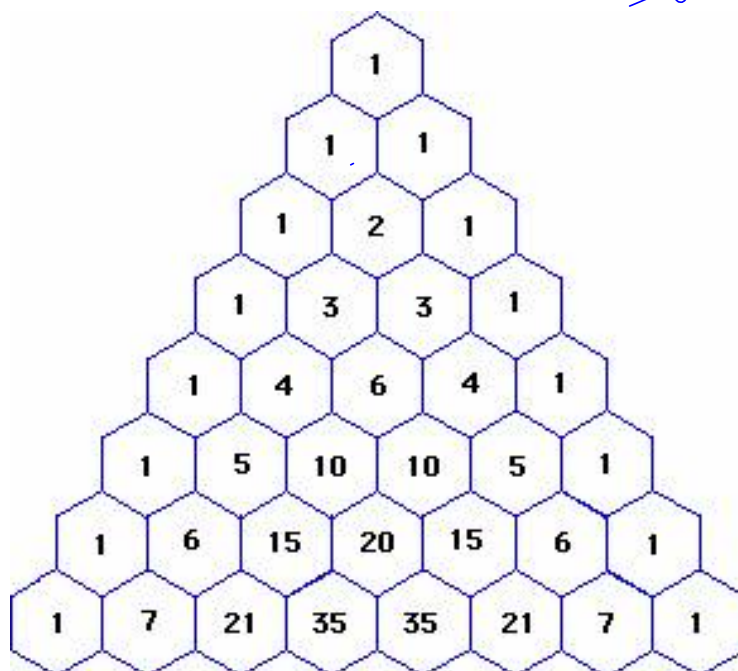
Pascal's Triangle - Counting Numbers



Pascal's Triangle - Triangle Numbers



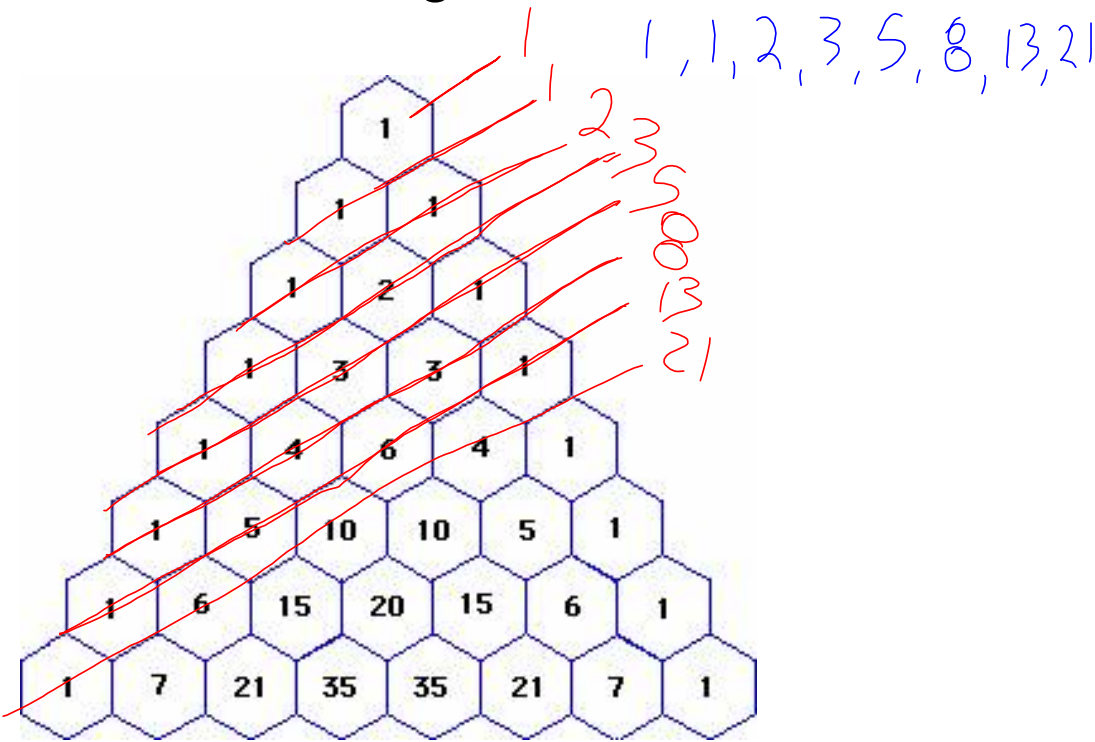
Pascal's Triangle - Powers of 2

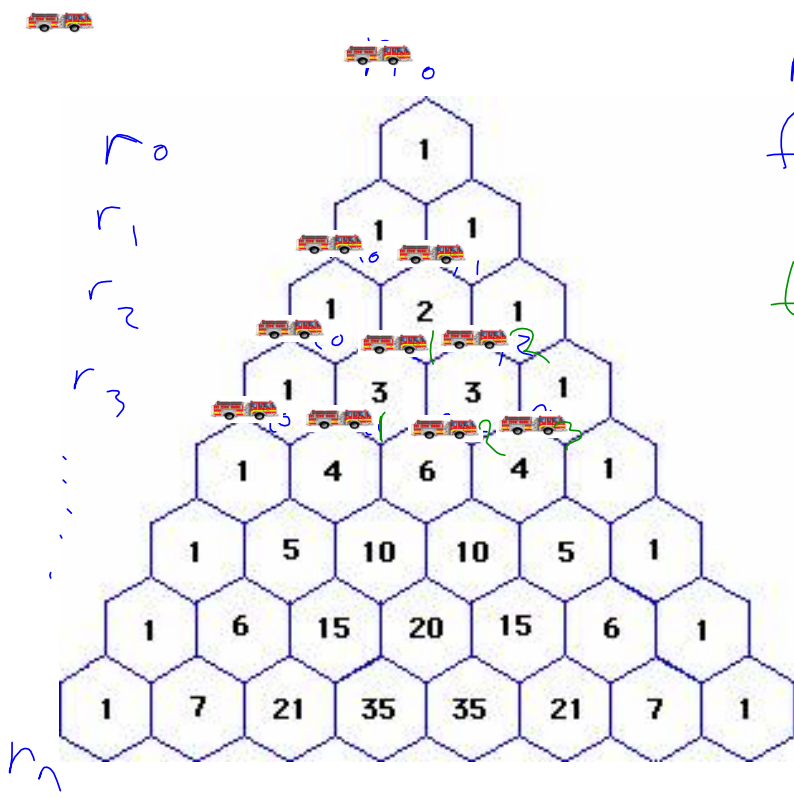


Sum of Row

1 2^0
 2 2^1
 4 2^2
 8 2^3
 16 2^4
 32 2^5
 64 2^6
 128 2^7

Pascal's Triangle - Fibonacci





recursive formula

$$t_{r, n} = t_{r-1, n-1} + t_{r-1, n}$$

Golden Ratio

$$= 1.617\text{-----}$$

	1	1	2	3	5	8	13	21
	✓	✓	✓	✓	✓	✓	✓	✓
RATIOS	1	2	1.5	1.666	1.6	1.625	1.615	

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